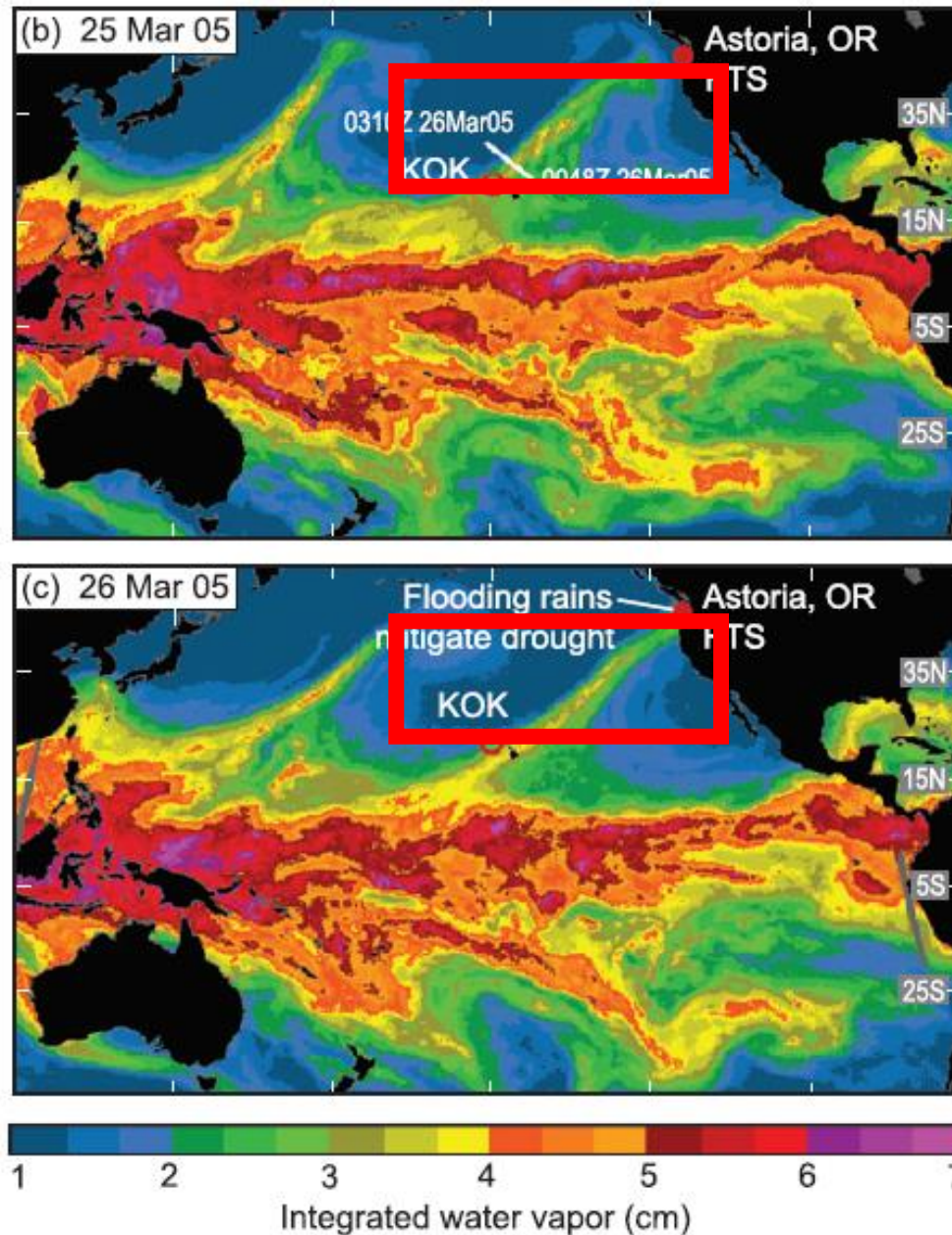


A moist static energy perspective on ARs

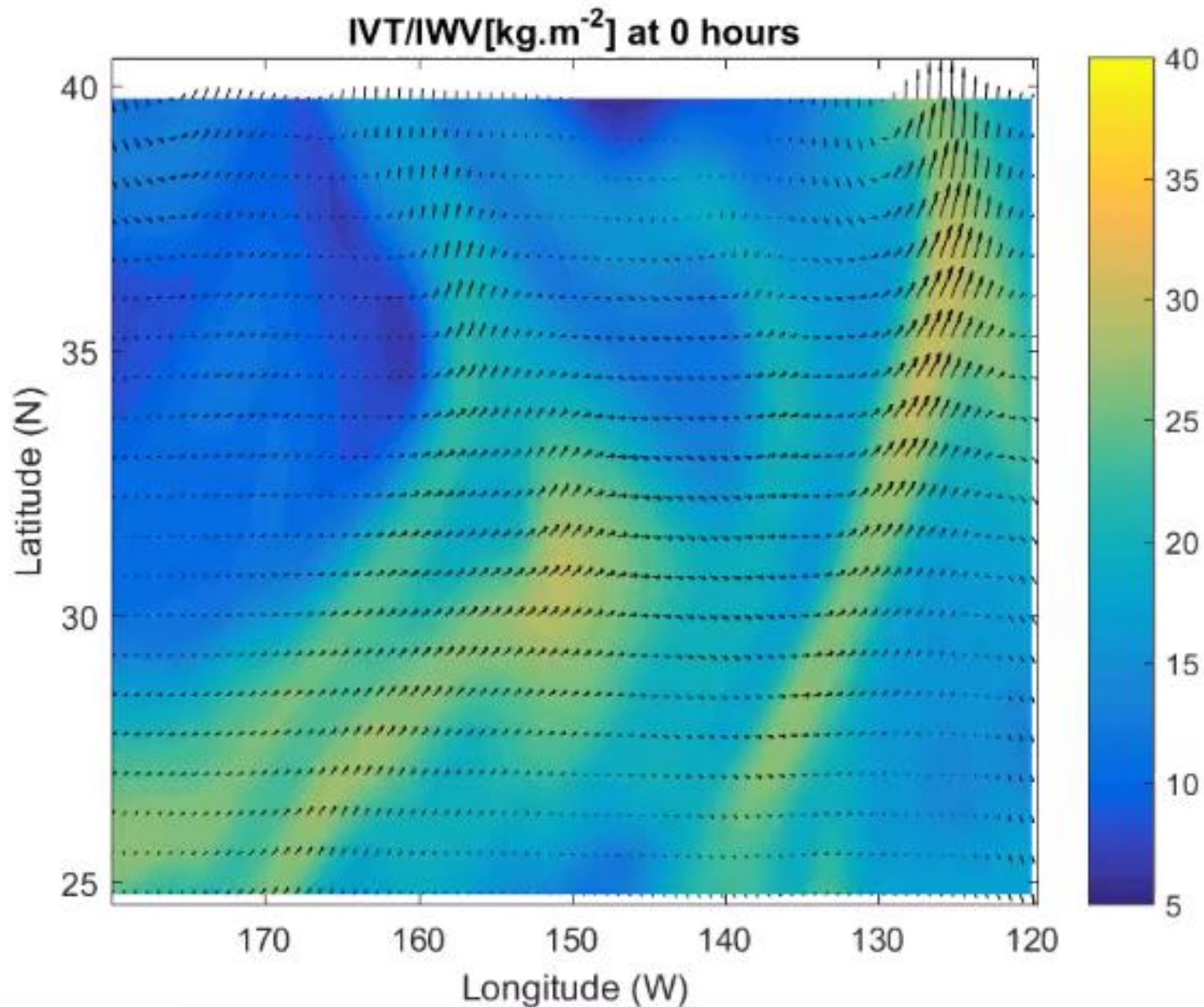
Tom BEUCLER



Pacific AR, Mar 05 (*Ralph et al., 2010*)

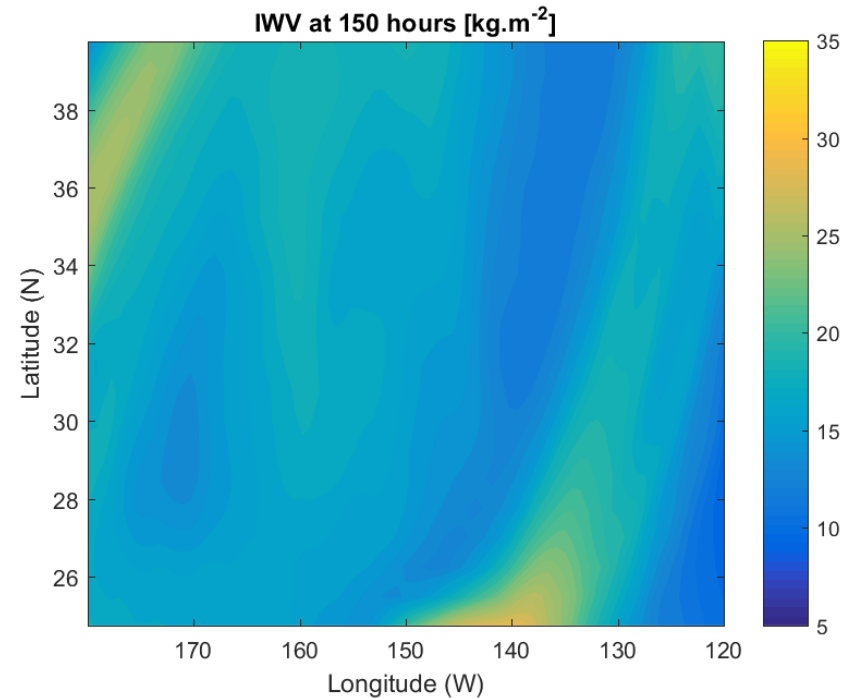
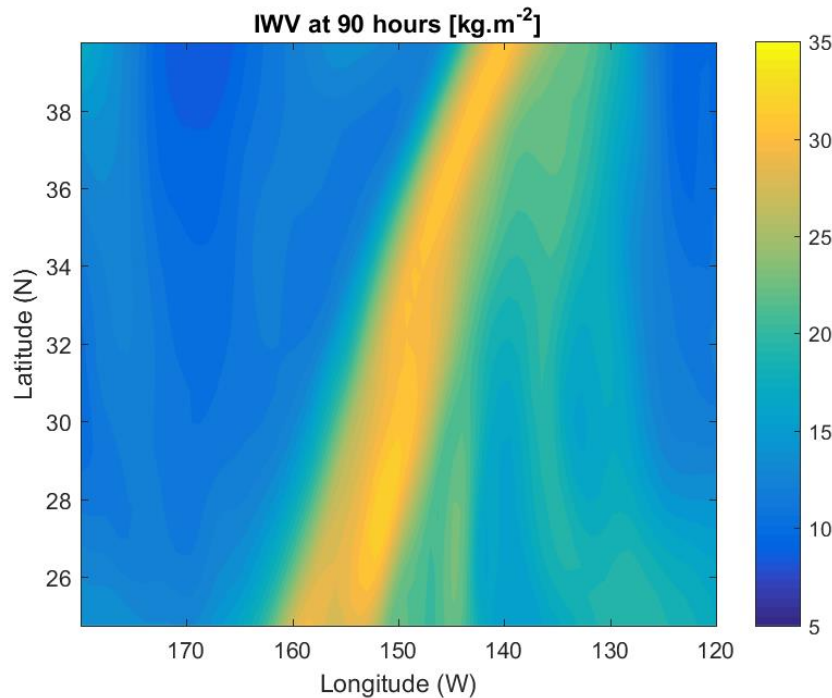


Colors: IWV Arrows: IVT

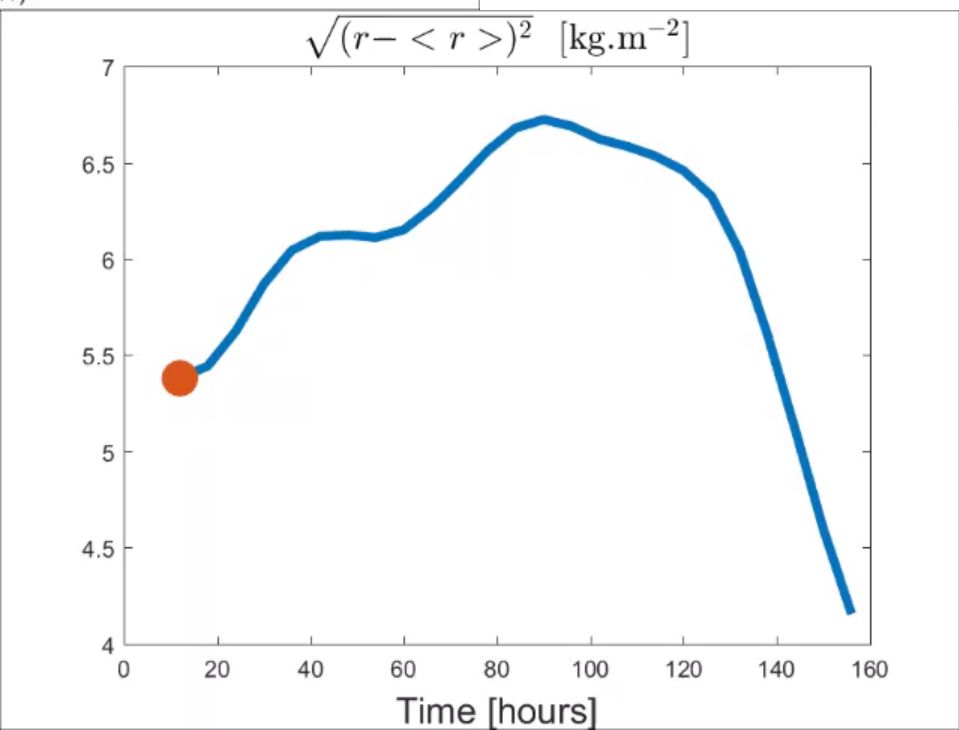
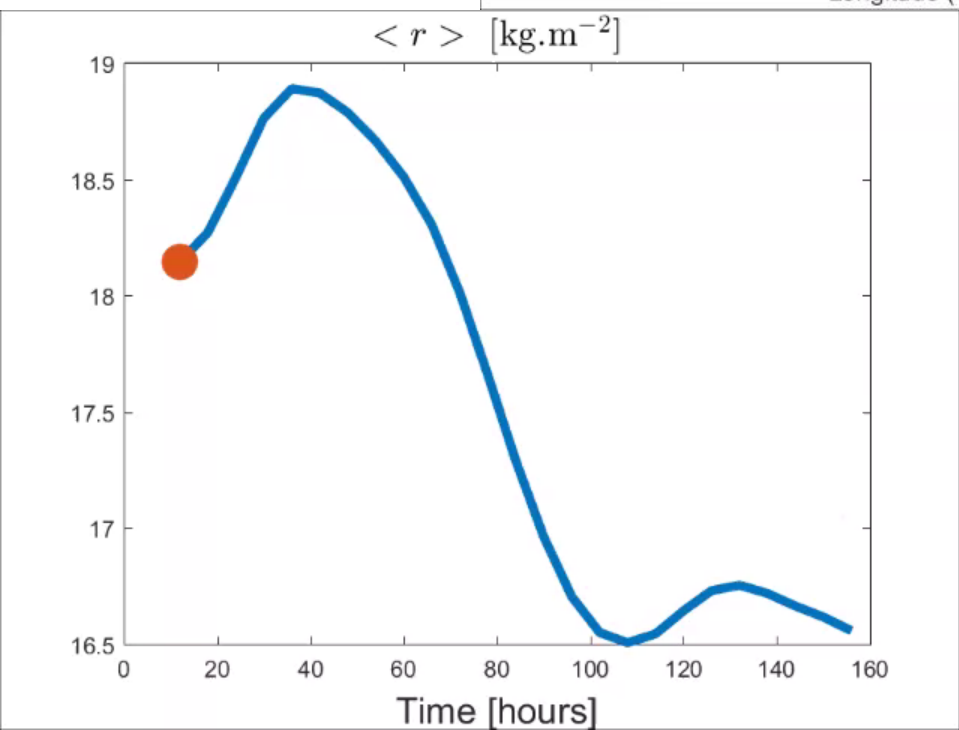
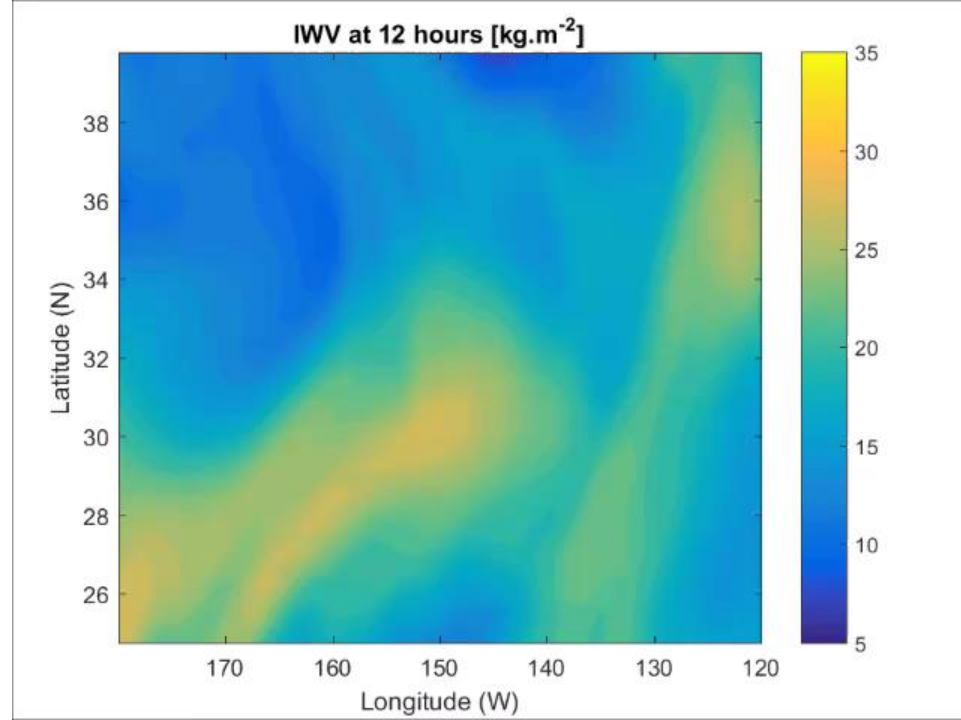


Goal

- Can we find simple physical variables to describe the AR structure within our domain?



- Domain-averaged IWV: $\langle r \rangle$
- Spatial standard deviation of IWV: $SD(r)$



Goal

- Can we find simple physical variables to describe the AR structure within our domain?
 - Domain-averaged IWV: $\langle r \rangle$
 - Spatial standard deviation: $SD(r)$
- **Problem**: Water vapor is not conserved
 - Requires knowledge of evaporation and precipitation at each pressure level
 - Need cloud resolving model with precise microphysics
- **Solution**: Variable conserved for adiabatic motion with water phase changes → **Moist static energy**

1. Moist static energy
2. Moist static energy variance
3. Comparison between Pacific cases

1. Moist static energy
2. Moist static energy variance
3. Comparison between Pacific cases

Definition

$$h = L_v r + c_p T + \Phi$$

Moist static energy Latent heat Sensible heat Geopotential

CONDENSATION

h is **conserved** for adiabatic motion
with water phase changes

➤ Unchanged by internal latent heating

Definition

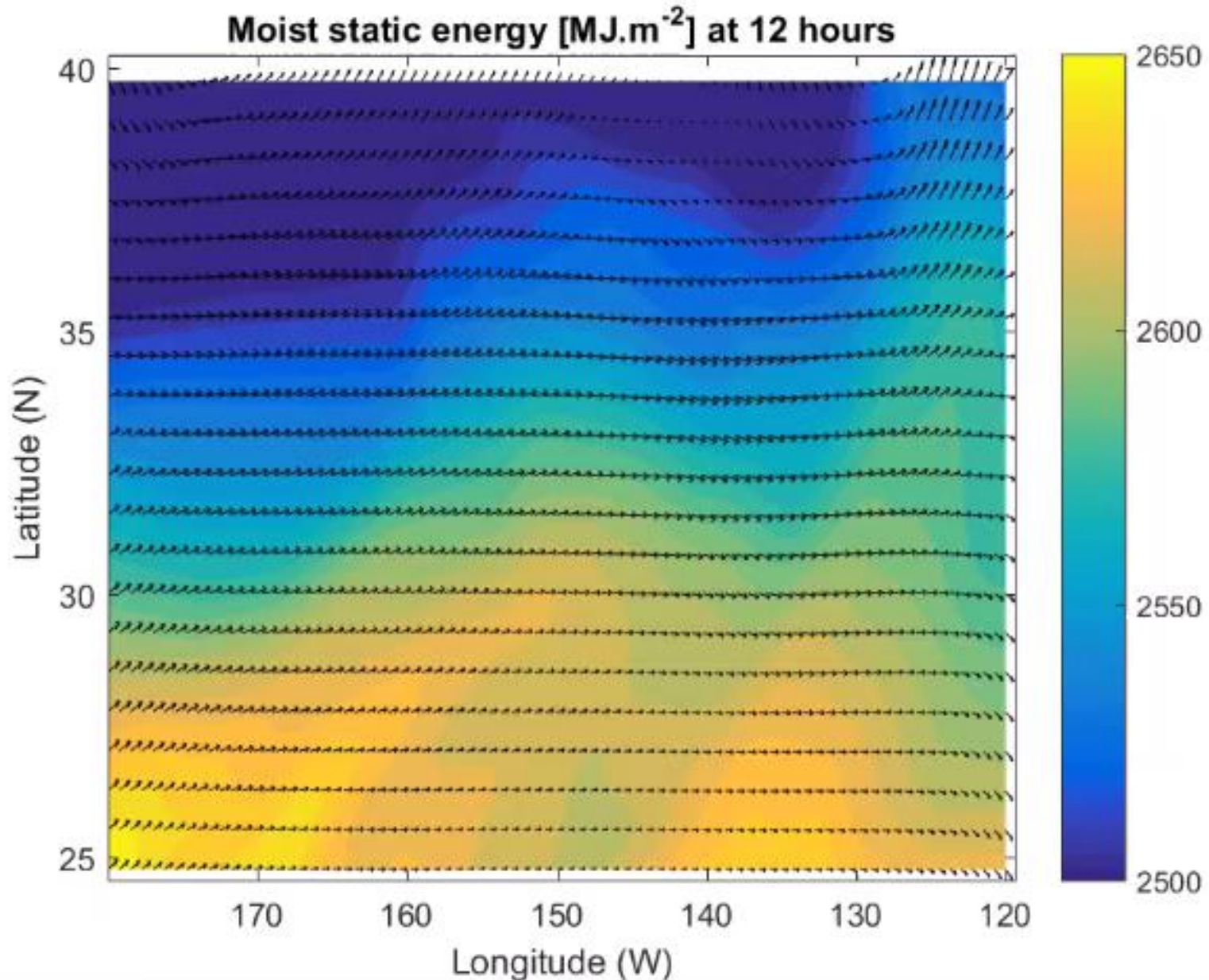
$$h = L_v r + c_p T + \Phi$$

Moist static energy Latent heat Sensible heat Geopotential

Column-integrated moist static energy:

$$\hat{h} \quad (J \cdot m^{-2})$$

Integrated moist static energy



Definition

$$\boxed{\hat{h}} = \boxed{L_v \hat{r}} + \boxed{c_p \hat{T}} + \boxed{\hat{\Phi}}$$

Integrated moist static energy

Integrated latent heat

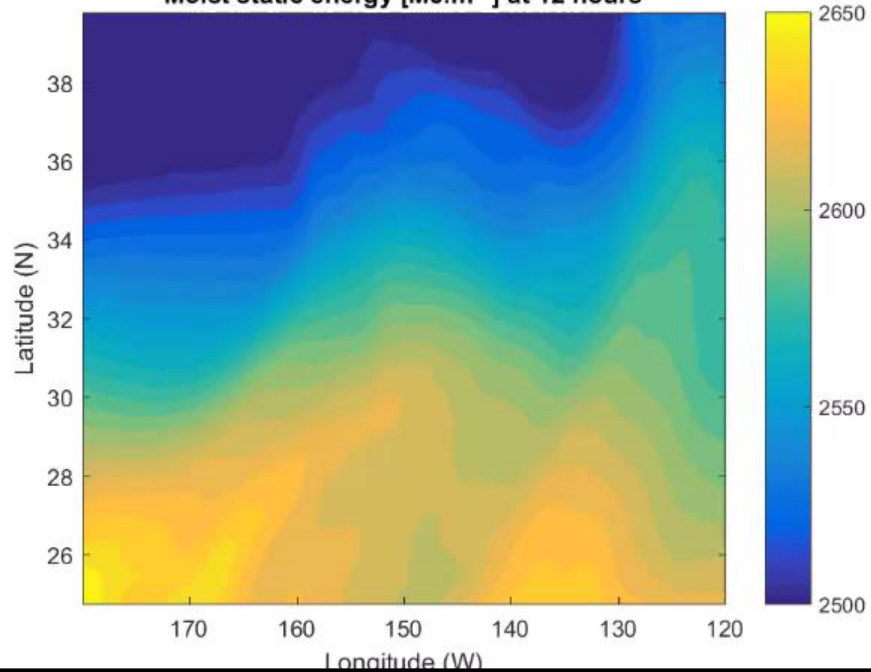
Integrated sensible heat

Integrated geopotential

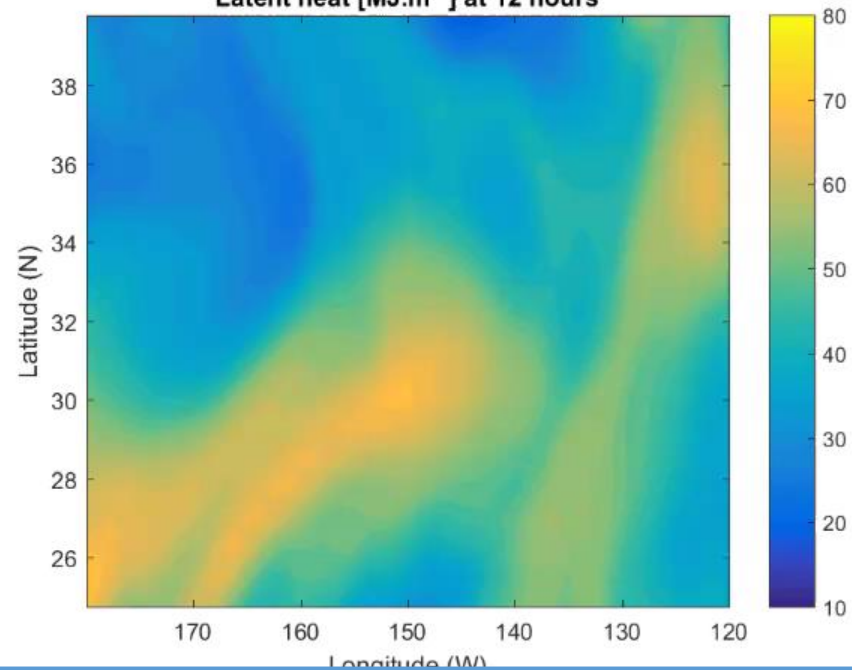
Column-integrated moist static energy:

$$\hat{h} \quad (J \cdot m^{-2})$$

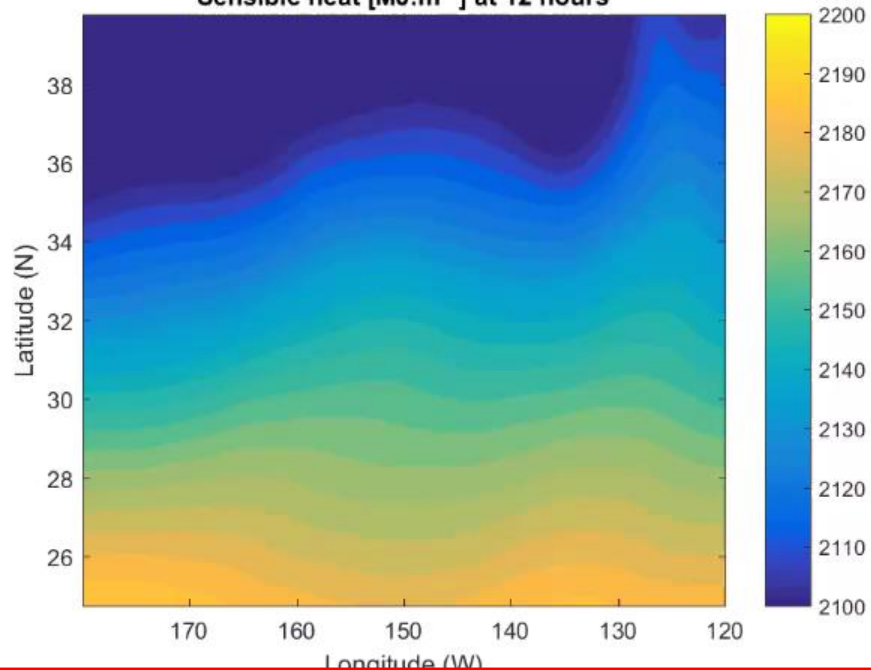
Moist static energy [MJ.m^{-2}] at 12 hours



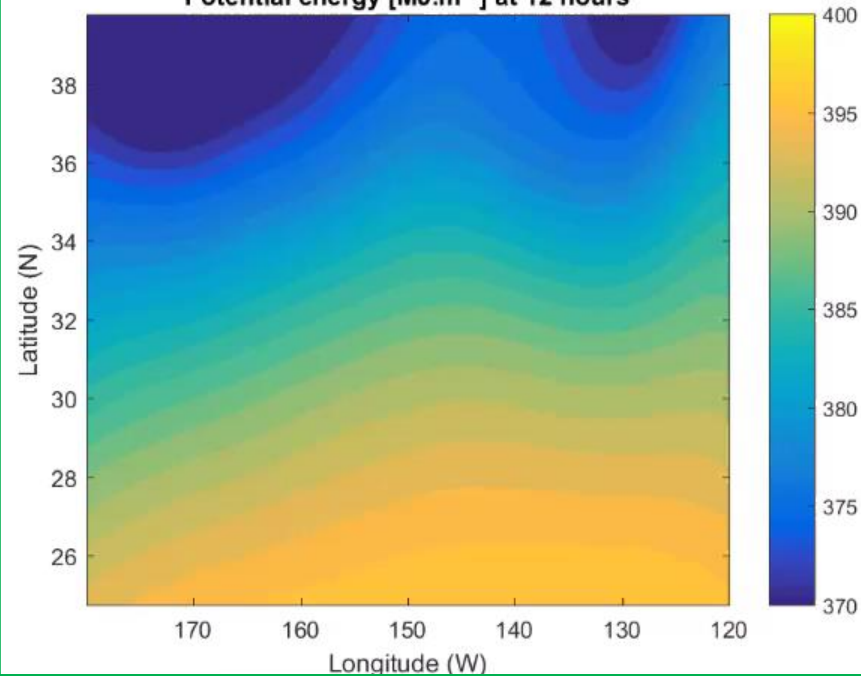
Latent heat [MJ.m^{-2}] at 12 hours



Sensible heat [MJ.m^{-2}] at 12 hours

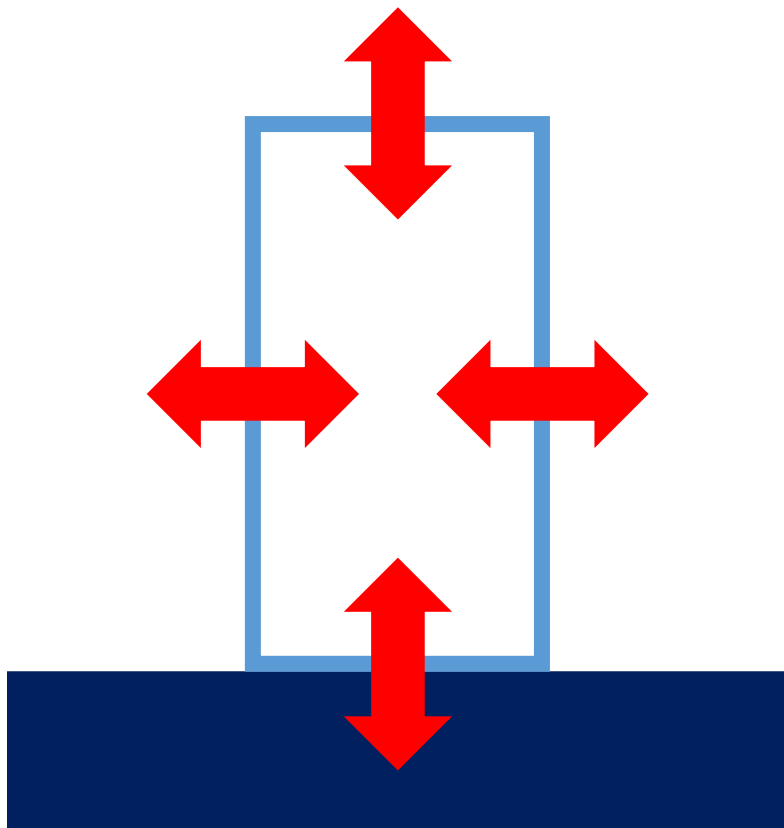


Potential energy [MJ.m^{-2}] at 12 hours



Integrated MSE budget

What changes $\hat{h}$ in our domain?



Net radiative fluxes

Lateral advection of
moist static energy

Surface turbulent fluxes

Integrated MSE budget

What changes $\hat{h}$ in our domain?

Local variation of MSE

$$\boxed{\frac{\partial \hat{h}}{\partial t}} = \boxed{-\vec{\nabla} \cdot h \vec{u}} + \boxed{\cancel{J_{\text{ext}}}}$$

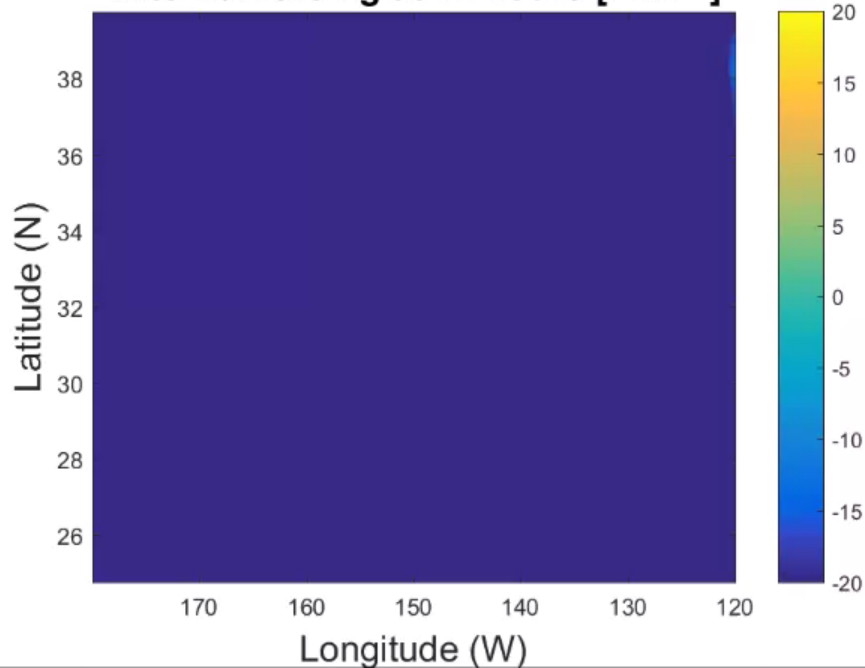
Lateral advection of MSE

External forcing

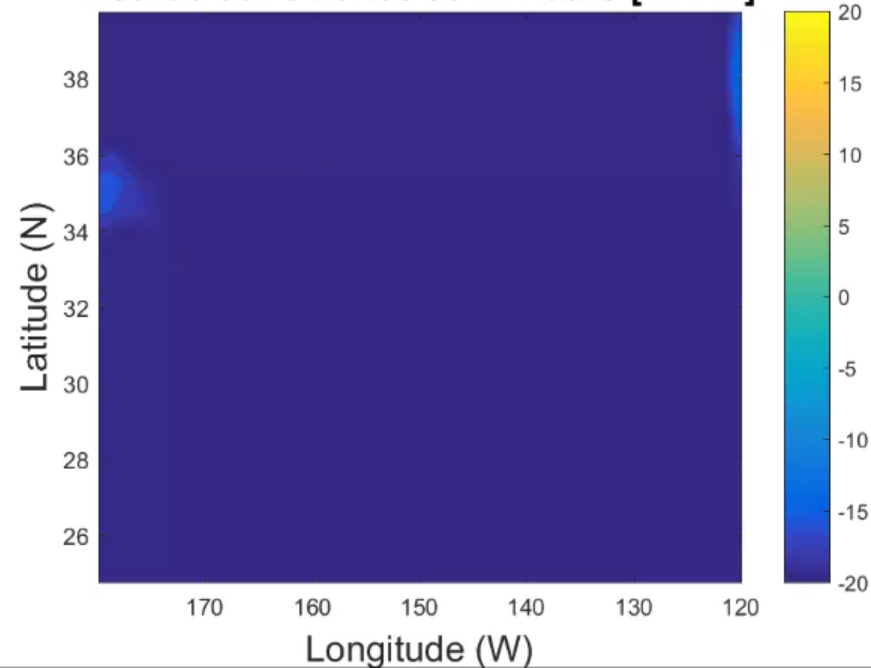
$\cancel{J_{\text{ext}}}$

$$= \text{Latent heat flux} + \text{Sensible heat flux} + \text{Net radiative cooling}$$

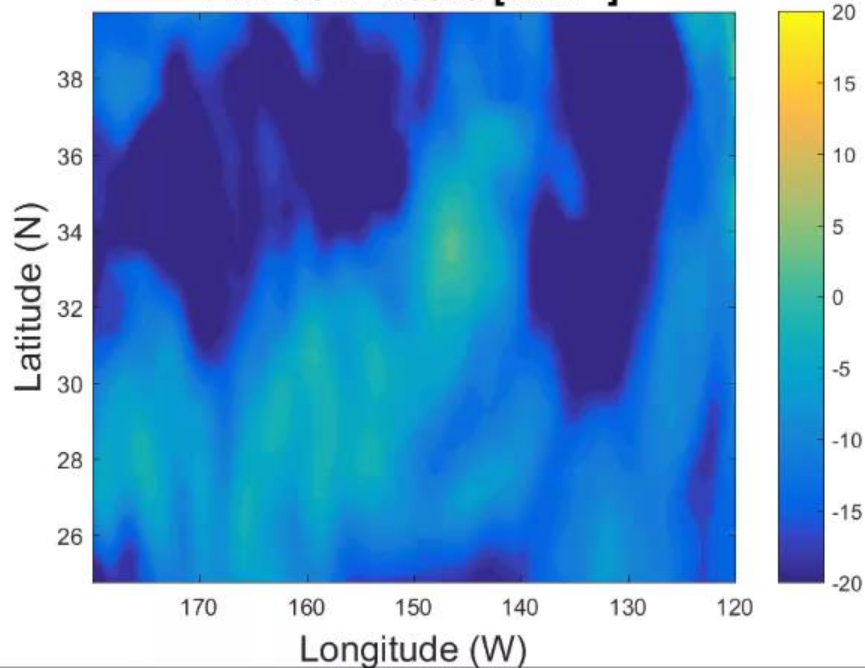
External forcing at 12 hours [W.m^{-2}]



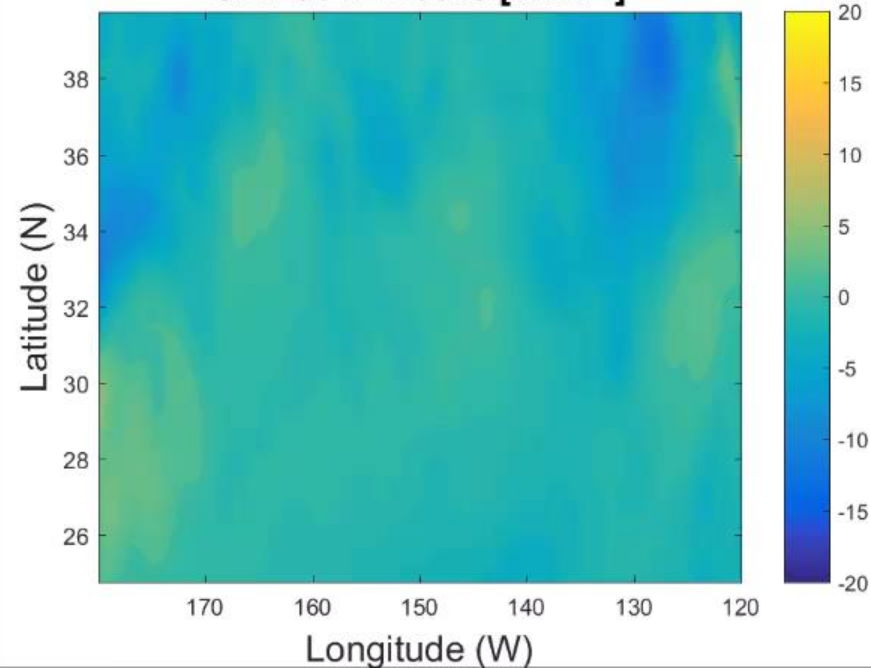
Net radiative fluxes at 12 hours [W.m^{-2}]



LHF at 12 hours [W.m^{-2}]



SHF at 12 hours [W.m^{-2}]



Integrated MSE budget

What changes $\hat{h}$ in our domain?

Local variation of MSE

$$\boxed{\frac{\partial \hat{h}}{\partial t}} = \boxed{-\vec{\nabla} \cdot h \vec{u}} + \boxed{\cancel{J_{\text{net}}}}$$

Lateral advection of MSE

External forcing

$\cancel{\text{External forcing}} = \text{Latent heat flux} + \text{Sensible heat flux} + \text{Net radiative cooling}$

Integrated MSE budget

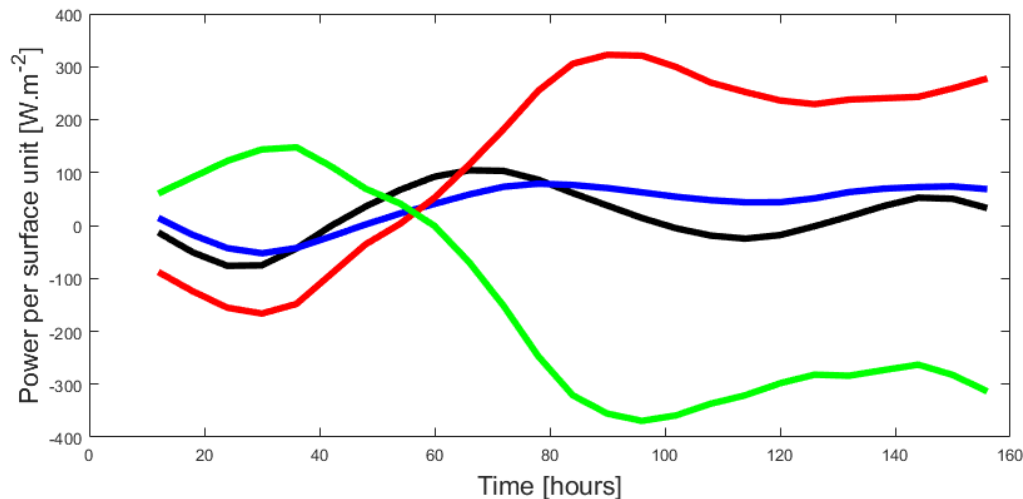
What changes $\hat{h}$ in our domain?

Local variation of MSE

$$\boxed{\frac{\partial \hat{h}}{\partial t}} \approx \boxed{-\vec{\nabla} \cdot r \vec{u}} + \boxed{H_{\text{ext}}}$$

Lateral advection of latent heat

External forcing



Sensible heat

Latent heat $\approx$ MSE

Potential energy

1. Moist static energy
2. Moist static energy variance
3. Comparison between Pacific cases

Moist static energy spatial variance

Domain average:

$$\langle \hat{h} \rangle$$

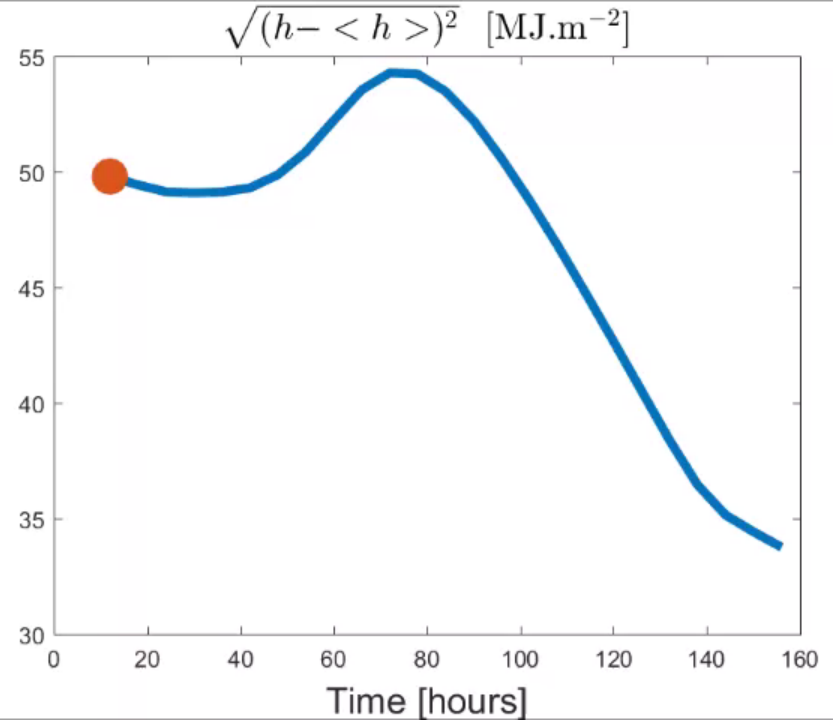
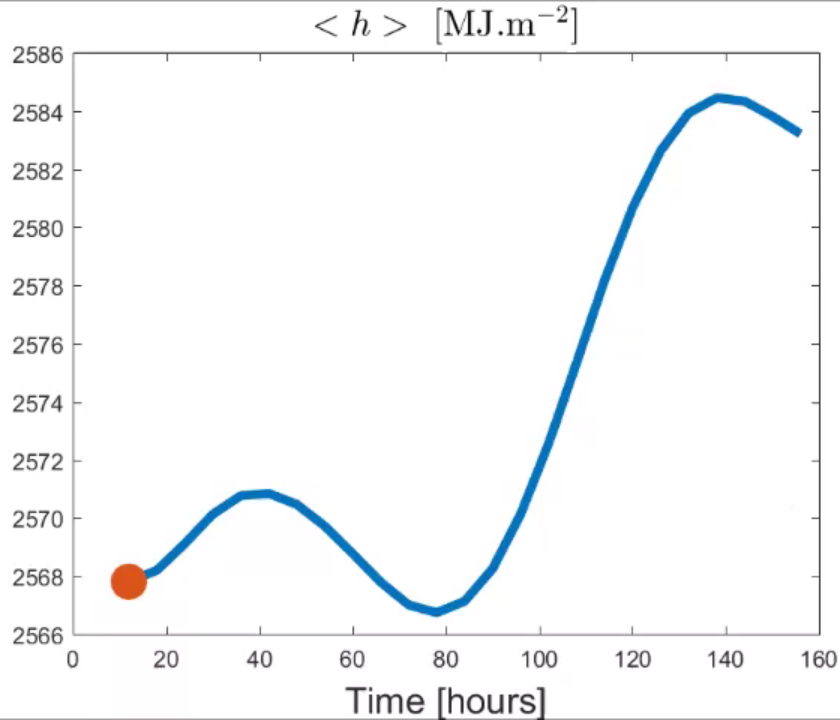
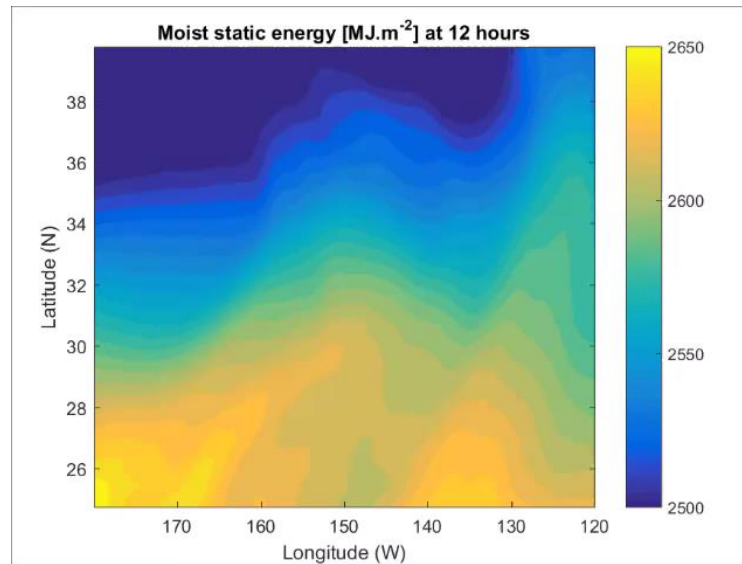
Perturbation:

$$\hat{h}' = \hat{h} - \langle \hat{h} \rangle$$

Spatial variance:

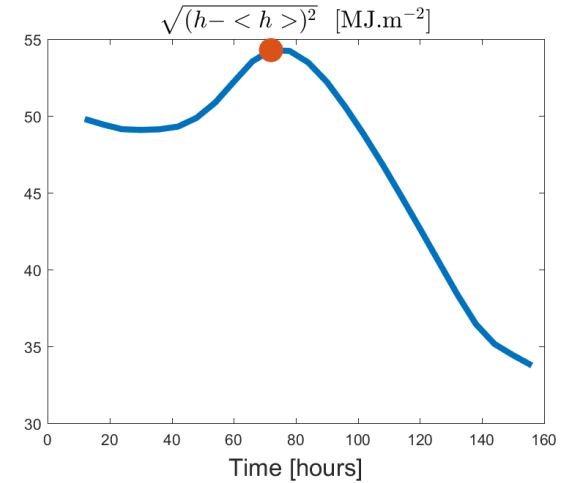
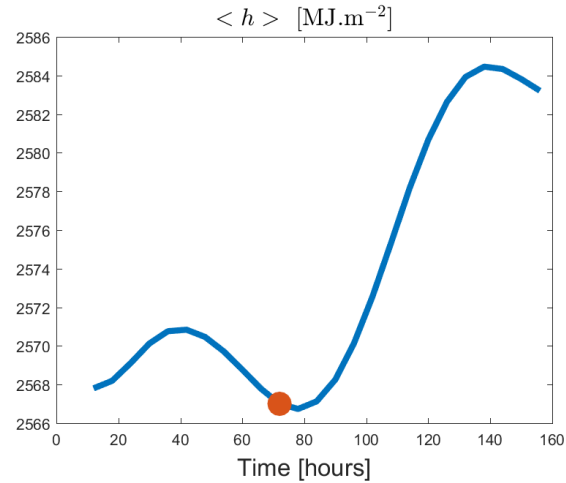
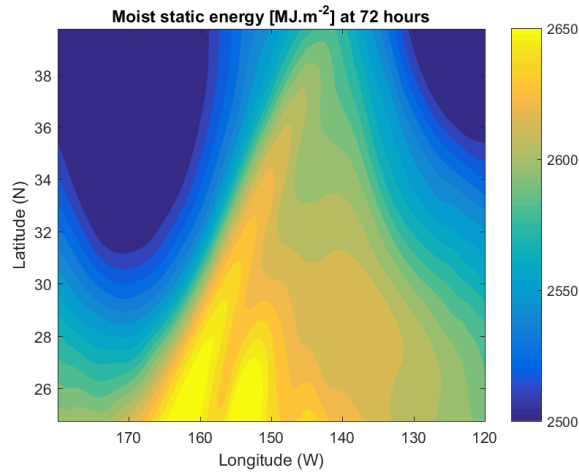
$$\langle \hat{h}'^2 \rangle$$

Moist static energy mean & St.Dev.

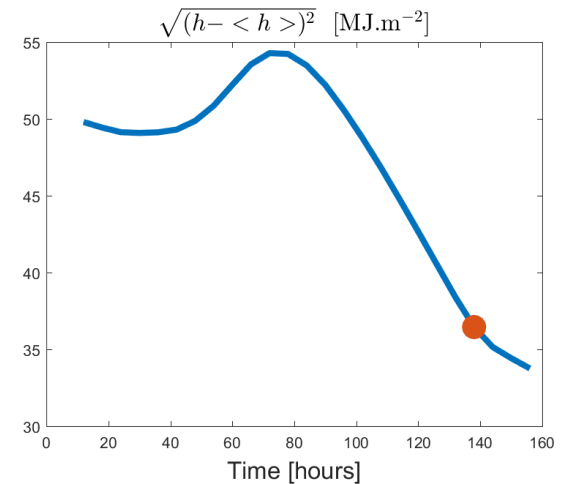
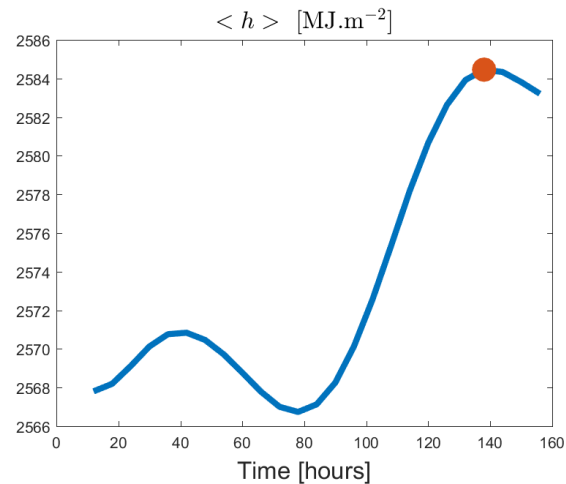
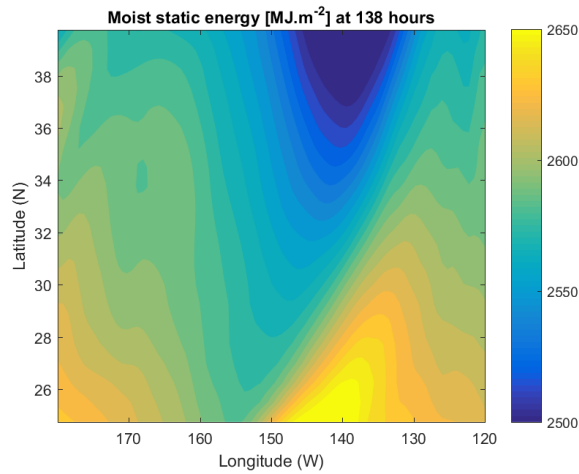


MSE variance is a better metric for AR

72 hours $\leftrightarrow$ Peak AR intensity



138 hours $\leftrightarrow$ End AR life



Budget of MSE variance (*Wing and Emanuel, 2014*)

What changes $\langle \hat{h}'^2 \rangle$ in our domain?

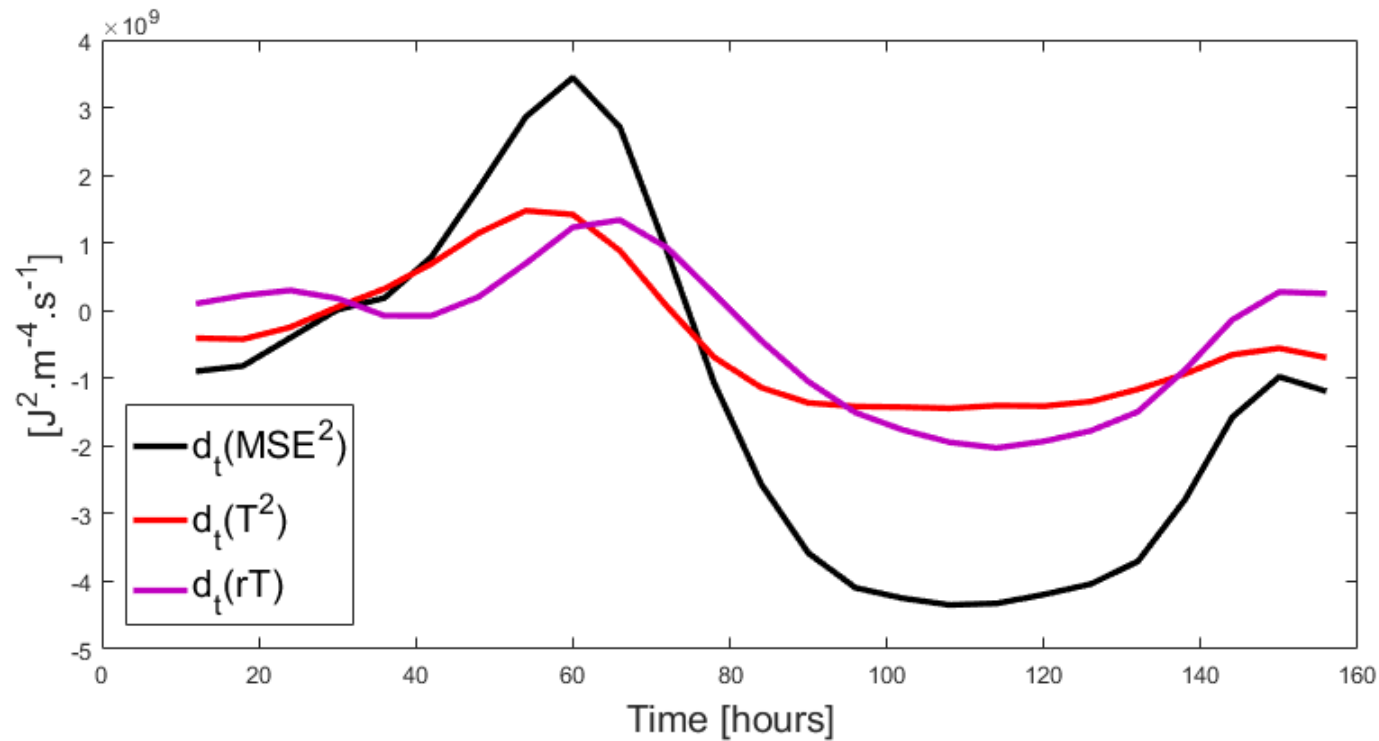


$$\boxed{\frac{\partial}{\partial t} \frac{\langle \hat{h}'^2 \rangle}{2}} = \boxed{- \langle \hat{h}' \left(\widehat{\vec{\nabla} \cdot h \vec{u}} \right)' \rangle} + \boxed{\langle \hat{h}' \text{ext} \rangle}$$

Local variation of MSE variance Correlation between MSE and MSE advection **Correlation between MSE and ext forcing**

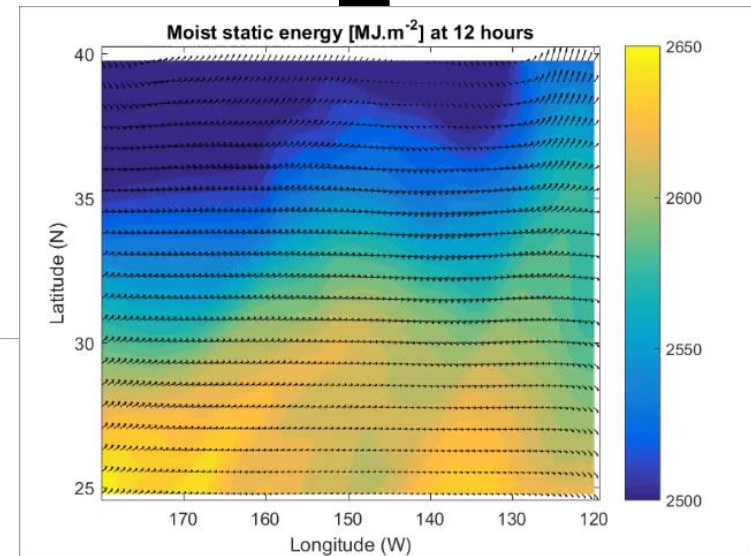
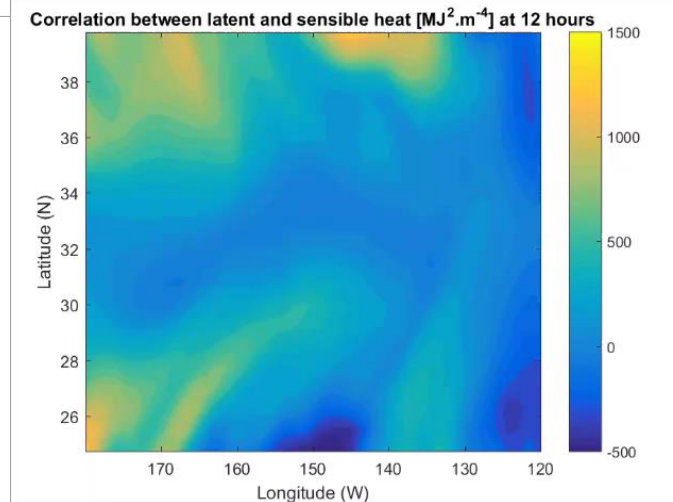
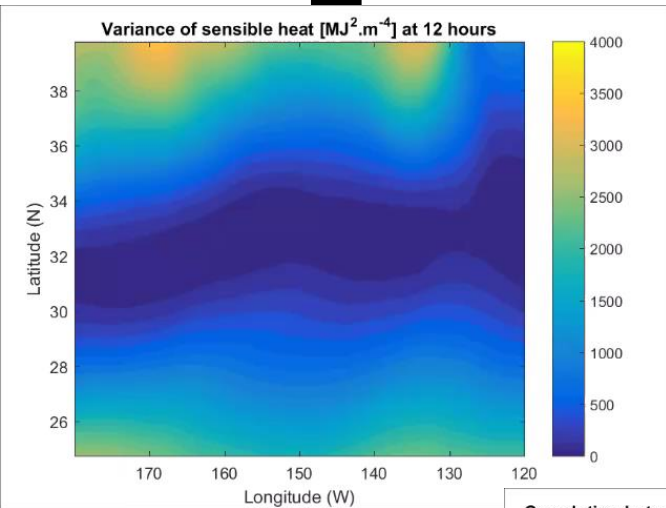
Decomposition of MSE var. tendency

$$\frac{\partial}{\partial t} \frac{\langle \hat{h}'^2 \rangle}{2} = \frac{\partial}{\partial t} \left\langle \cancel{\frac{(L_v \hat{r}')^2}{2}} + \frac{(c_p \hat{T}')^2}{2} + \cancel{\frac{(\hat{\phi}')^2}{2}} + \cancel{\frac{(L_v \hat{r}') (c_p \hat{T}')}{2}} + \cancel{\frac{(L_v \hat{r}') (\hat{\phi}')}{2}} + \cancel{\frac{(\hat{\phi}') (c_p \hat{T}')}{2}} \right\rangle$$



Final AR budget

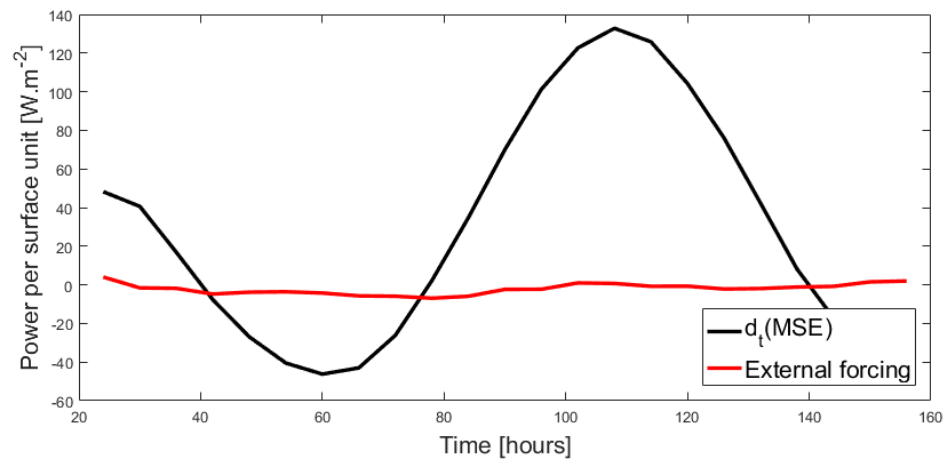
$$\frac{\partial}{\partial t} < \underbrace{\frac{(c_p \hat{T}')^2}{2}}_{\text{Variance of sensible heat}} + \underbrace{(L_v \hat{r}')(c_p \hat{T}')}_{\text{Correlation between latent and sensible heat}} > = < \hat{h}' \cdot \underbrace{\left(\vec{\nabla} \cdot L_v r \vec{u} \right)'}_{\text{Moist static energy}} >$$



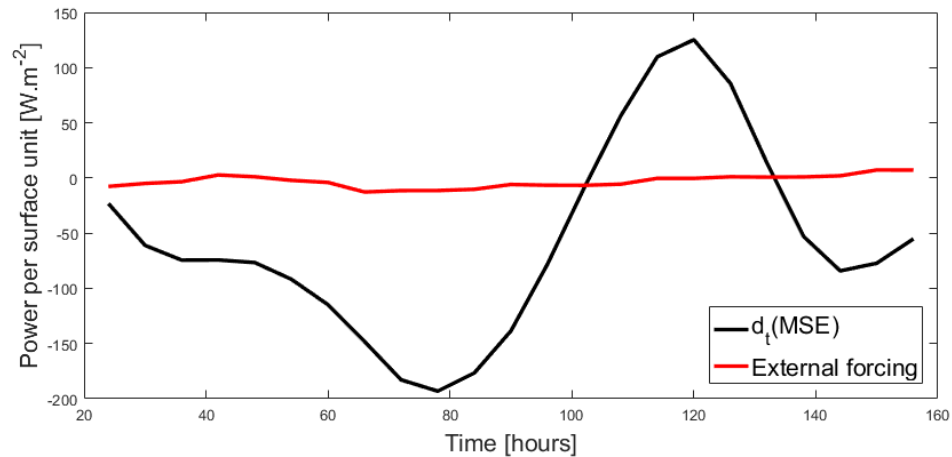
1. Moist static energy
2. Moist static energy variance
3. **Comparison between Pacific cases**

Summary

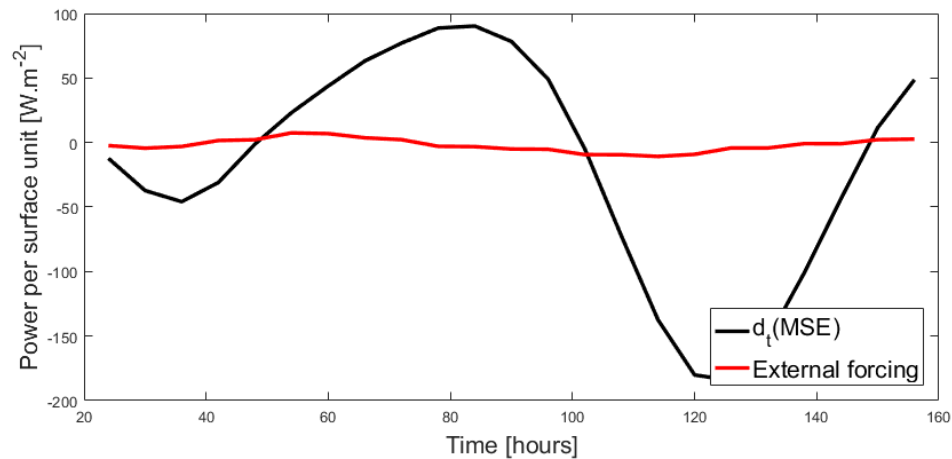
1. The external forcing is small



Mar 22, 2005



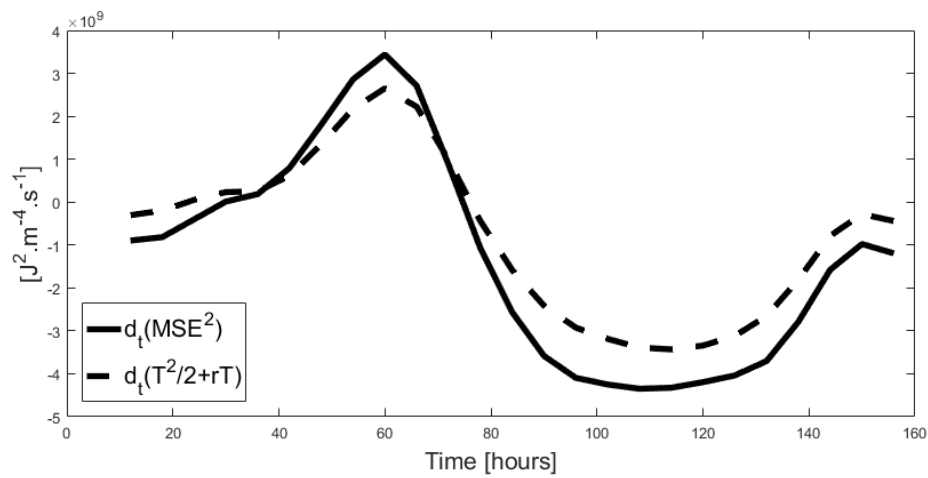
Feb 07, 2014



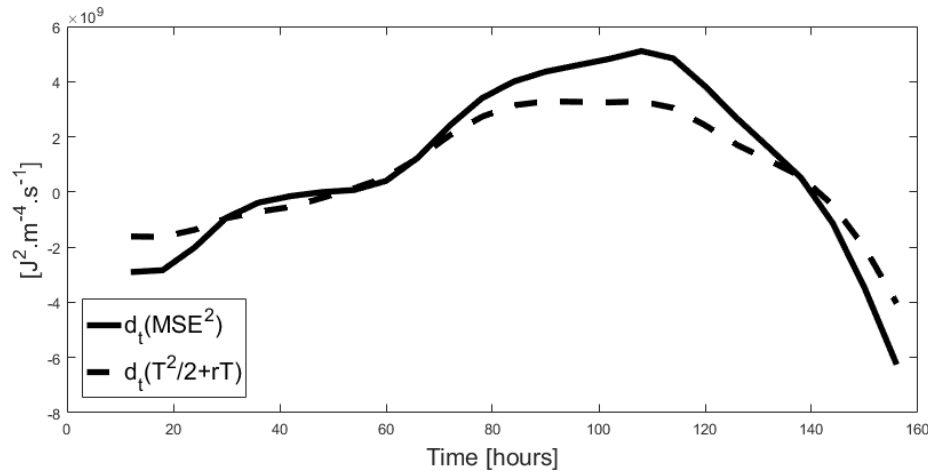
Nov 11, 2014

Summary

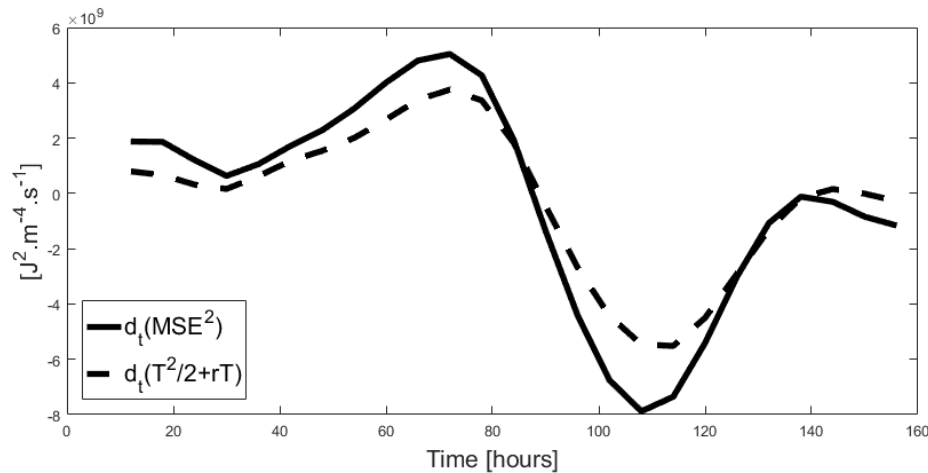
1. The external forcing is small
2. MSE var. $\approx$ Latent/Sensible heat var.



Mar 22, 2005



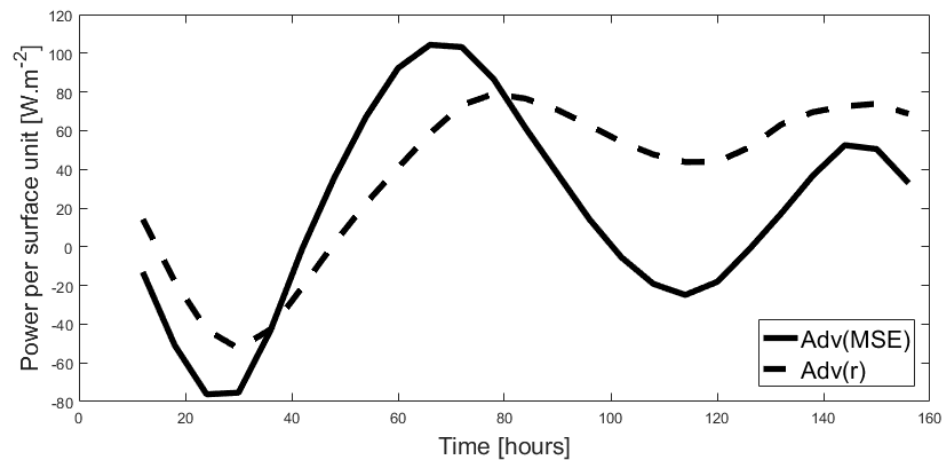
Feb 07, 2014



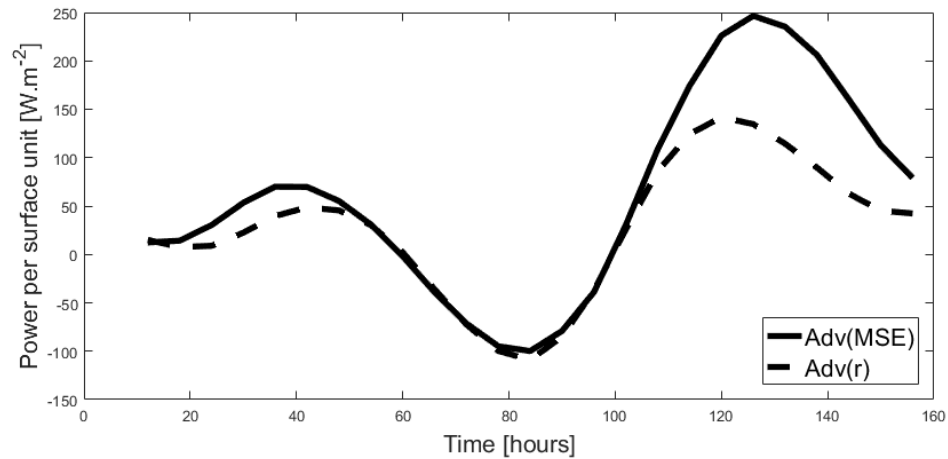
Nov 11, 2014

Summary

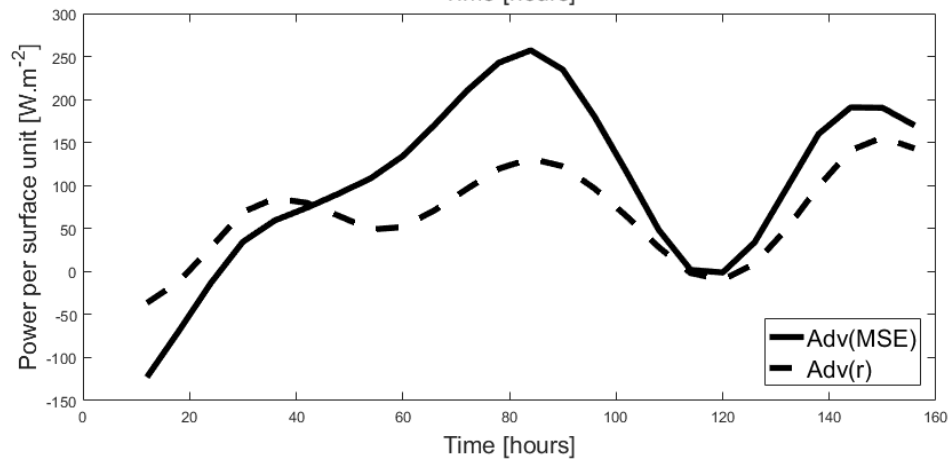
1. The external forcing is small
2. MSE var. $\approx$ Latent/Sensible heat var.
3. MSE adv. $\approx$ Latent heat advection



Mar 22, 2005



Feb 07, 2014

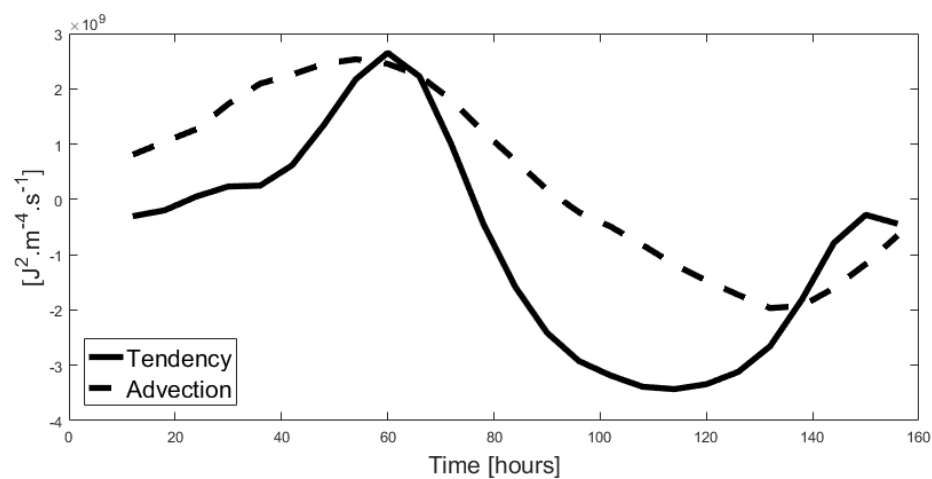


Nov 11, 2014

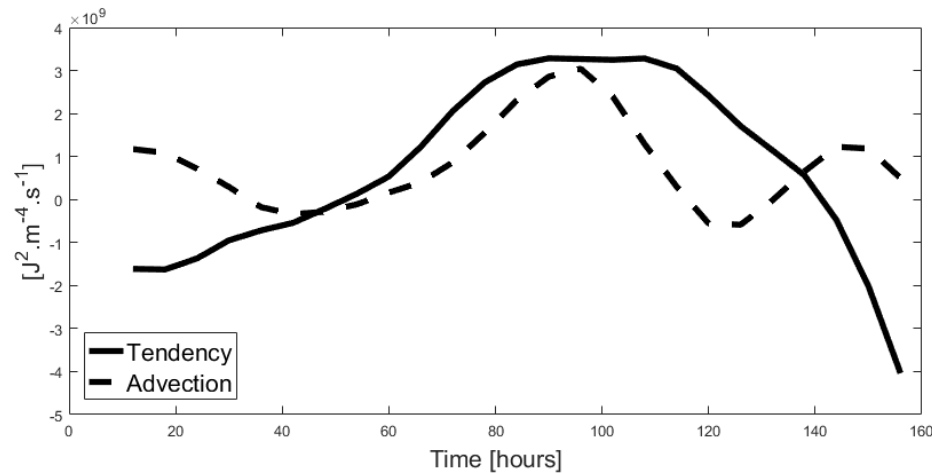
Summary

1. The external forcing is small
2. MSE var. $\approx$ Latent/Sensible heat var.
3. MSE adv. $\approx$ Latent heat advection
4. MSE variance budget:

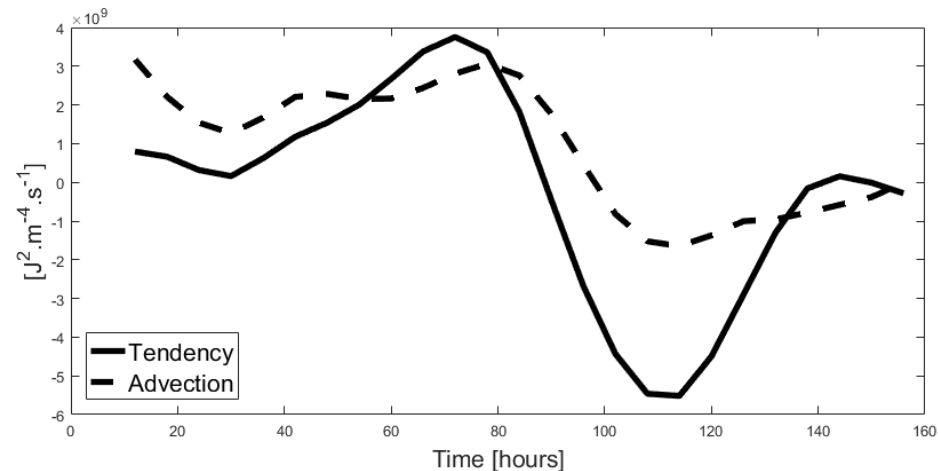
$$\frac{\partial}{\partial t} \frac{\langle \hat{h}'^2 \rangle}{2} = - \langle \hat{h}' \left(\widehat{\vec{\nabla} \cdot h \vec{u}} \right)' \rangle + \langle \hat{h}' F'_{ext} \rangle$$



Mar 22, 2005



Feb 07, 2014



Nov 11, 2014

Summary

1. The external forcing is small
2. MSE var. $\approx$ Latent/Sensible heat var.
3. MSE adv. $\approx$ Latent heat advection
4. AR budget:

$$\frac{\partial}{\partial t} \left\langle \frac{(c_p \hat{T}')^2}{2} + (L_v \hat{r}') (c_p \hat{T}') \right\rangle = \left\langle \hat{h}' \cdot \left(\vec{\nabla} \cdot \widehat{L_v r \vec{u}} \right)' \right\rangle$$